# Average Co magnetic moment of R-Co-B (R = Y, Pr and Nd) compounds

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We estimate the average Co magnetic moment and account for the moment variation by a model in  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ),  $Pr_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 1 and m = 2, n = 3),  $Nd_{m+n}Co_{5m+3n}B_{2n}$  (m = 3, n = 2) and  $Y_2Co_{14}B$  compounds. And we obtain the magnetic properties of hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (n = 1, m = 2, 3, 4 and 5) compounds. © 2005 Springer Science + Business Media, Inc.

## 1. Introduction

In the case of R-Co-B (R = rare-earth) systems, it has been shown that a homologous series of compounds exists between the compositions RCo<sub>5</sub> and RCo<sub>3</sub>B<sub>2</sub>. This series is represented by a general formula  $R_{n+1}Co_{3n+5}B_{2n}$ , which is formed by alternating stacking of one layer RCo<sub>5</sub> and *n* layers RCo<sub>3</sub>B<sub>2</sub> along the *c* axis. The  $R_{n+1}Co_{3n+5}B_{2n}$  compounds, where *R* is a rare earth or yttrium, crystallize in a hexagonal structure having the P6/mmm space group and are known to exhibit a very interesting series of crystal structures with special atomic orderings depending on n [1–3]. The crystal structures of  $R_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1,2, 3 and  $\infty$ ),  $R_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 1 and m = 2, n = 3) and R<sub>2</sub>Co<sub>14</sub>B are shown in Fig. 1. The  $R_{n+1}Co_{3n+5}B_{2n}$  compounds with n = 1 (RCo<sub>4</sub>B), n = 2 (R<sub>3</sub>Co<sub>11</sub>B<sub>4</sub>), n = 3 (R<sub>2</sub>Co<sub>7</sub>B<sub>3</sub>) and  $n = \infty$ (RCo<sub>3</sub>B<sub>2</sub>) are derived from the RCo<sub>5</sub> structure by substituting *B* for Co at the 2c site [4]. For  $R_{n+1}Co_{3n+5}B_{2n}$ , there are three kinds of Co sites expressed by Co(N) with N = 1, 2 and 3, where Co(N) means a Co atom which has N boron layers just above and/or just below. The  $RCo_4B$  compound has Co(0) and Co(1) sites. The  $R_3Co_{11}B_4$  and  $R_2Co_7B_3$  compounds have Co(0), Co(1)and Co(2) sites. The RCo<sub>3</sub>B<sub>2</sub> compound has only Co(2)site and the average Co moment is very small [5].

New compounds  $R_3Co_{13}B_2$  (R = Pr, Nd and Sm) [6–8],  $R_5Co_{19}B_6$  (R = Pr and Nd) [6, 9] and Nd<sub>5</sub>Co<sub>21</sub>B<sub>4</sub> [10] have been synthesized successfully and belong to the  $R_{m+n}Co_{5m+3n}B_{2n}$  family with m = 2, n = 1, m = 2, n = 3 and m = 3, n = 2, respectively. The crystal structure of m = 3, n = 2 is the same as that of m = 2, n = 3. While the 2*d* and 4*h*2 sites are occupied by *B* and the 4*h*1 site is occupied by Co in m = 2, n = 3, those by Co and that by *B* in m = 3, n = 2. Those crystallize in a hexagonal structure having the P6/mmm space group and are crystal-lographically equivalent to  $R_{n+1}Co_{3n+5}B_{2n}$ , which is  $R_{m+n}Co_{5m+3n}B_{2n}$  with m = 1. Those are formed by alternate stacking of *m* parts of RCo<sub>5</sub> with *n* parts of RCo<sub>3</sub>B<sub>2</sub> along the *c* axis and are expected to show a

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combination of high Curie temperature, large saturation magnetization and large magnetocrystaline anisotropy. The  $R_3Co_{13}B_2$  and  $R_5Co_{21}B_4$  compounds have Co(0) and Co(1) sites. The  $R_5Co_{19}B_6$  compound has Co(0), Co(1) and Co(2) sites.

The R<sub>2</sub>Co<sub>14</sub>B compound crystallizes with a tetragonal structure having the P42/mnm space group and has two rare-earth sites (4f and 4g), six Co sites (16k1, 16k2, 8j1, 8j2, 4e and 4c) and one boron site (4g). The R<sub>2</sub>Fe<sub>14</sub>B compound is most attractive due to the industrial application for permanent magnets. There are four  $R_2Co_{14}B$  units (68 atoms) per unit cell. All the R and B atoms, but only 4 of the 56 Co atoms, reside in the z = 0 and 0.5 planes. Between these the other Co atoms form puckered, yet fully connected, hexagonal nets. The tetragonal structure of R<sub>2</sub>Co<sub>14</sub>B is closely related to the RCo<sub>5</sub>-type structure [11]. The B atom occupies the center of trigonal prism formed by the three nearest Co atoms above and the three below the plane containing B and R atoms. The prisms are strong structural units linking the Co planes above and below those containing R and B [12]. The prisms also coordinate all R and B atoms. Three R atoms are bonded to each B through the rectangular prism faces. Gaskell [13] has stressed that such trigonal prisms are fundamental to the structure of many transition metal-metalloid systems, both crystalline (e.g., FeB and Fe<sub>3</sub>C) and amorphous.

In this work, we estimate the average Co magnetic moment and account for the moment variation by a model in  $Y_{n+1}Co_{3n+5}B_{2n}$   $(n = 0, 1, 2, 3 \text{ and } \infty)$ ,  $Pr_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 1 and m = 2, n = 3),  $Nd_{m+n}Co_{5m+3n}B_{2n}$  (m = 3, n = 2) and  $Y_2Co_{14}B$  compounds. And we obtain the magnetic properties of hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (n = 1, m = 2, 3, 4 and 5) compounds.

## 2. Results and discussion

# 2.1. Interatomic distance

We calculated the distances from each site to the neighboring atoms, d, and the number of the neighboring



Figure 1 The crystal structure of  $R_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ),  $R_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 1 and m = 2, n = 3) and  $R_2Co_{14}B$ .

atoms at each site, N, in  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3and  $\infty$ ),  $Pr_3Co_{13}B_2$ ,  $Pr_5Co_{19}B_6$  and  $Y_2Co_{14}B$ . We used the results of Rietveld refinement for  $Y_{n+1}Co_{3n+5}B_{2n}$ (n = 0, 1, 2, 3 and  $\infty$ ) [14],  $Pr_3Co_{13}B_2$  [6],  $Pr_5Co_{19}B_6$ [8] and Nd<sub>2</sub>Fe<sub>14</sub>B [11] and the values of the lattice constants for  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ),  $Pr_3Co_{13}B_2$ ,  $Pr_5Co_{19}B_6$  and  $Y_2Co_{14}B$ , which are from Refs. [5, 6, 8, 15], respectively. We also calculated the average distance from each Y (Pr), Co and B site to the neighboring Y (Pr), Co and B.

The dependence of the average distances from each Co site to the neighboring Co and B atoms,  $d_{Co-Co}$ and  $d_{Co-B}$ , and from each B site to the neighboring B atoms,  $d_{B-B}$  on the *B* concentration for  $Y_{n+1}Co_{3n+5}B_{2n}$  $(n = 0, 1, 2, 3 \text{ and } \infty)$ , Pr<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Pr<sub>5</sub>Co<sub>19</sub>B<sub>6</sub> and Y<sub>2</sub>Co<sub>14</sub>B is shown in Fig. 2. The values of d<sub>Co-Co</sub> and  $d_{Co-B}$  increase with increasing B concentration. The increase in d<sub>Co-Co</sub> is larger than that in d<sub>Co-B</sub>. The values of  $d_{B-B}$  decrease with increasing *B* concentration. The density, D, of  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3) and  $\infty$ ), Y<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Y<sub>5</sub>Co<sub>19</sub>B<sub>6</sub> and Y<sub>2</sub>Co<sub>14</sub>B is also shown in Fig. 2. When we calculated the values of Y<sub>3</sub>Co<sub>13</sub>B<sub>2</sub> and Y<sub>5</sub>Co<sub>19</sub>B<sub>6</sub>, we used the lattice constants of  $Pr_3Co_{13}B_2$  and  $Pr_5Co_{19}B_6$ . The values of D decrease linearly with increasing B concentration and those of  $Y_3Co_{13}B_2$ ,  $Y_5Co_{19}B_6$  and  $Y_2Co_{14}B$  are small in spite of small B concentration.

In  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 1, 2, 3 and  $\infty$ ),  $Pr_3Co_{13}B_2$ ,  $Pr_5Co_{19}B_6$  and  $Y_2Co_{14}B$ , trigonal prism containing B atom exists and that in the YCo<sub>4</sub>B structure is shown in Fig. 3. The B atom occupies the center of trigonal prism formed by the three nearest Co atoms above and the three below the plane containing B and R. The distances between the B(2d) atom and its nearest neighbors are B-Co(6i) = 2.05 Å, B-Co(6i) = 2.08 Å, B-Y(1b) = 2.92 Å and B-Y(1b) = 2.88 Å. The vertical edge length is Co(6i)-Co(6i) = 2.93 Å. Distance in the triangular face is Co(6i)-Co(6i) = 2.51 Å. The values above are almost the same values in  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 2, 3 and  $\infty$ ), Pr<sub>3</sub>Co<sub>13</sub>B<sub>2</sub> and Pr<sub>5</sub>Co<sub>19</sub>B<sub>6</sub>. In Y<sub>2</sub>Co<sub>14</sub>B, the distances between the B(4g) atom and its nearest neighbors are B-Co(16k1) = 2.02 Å, B-Co(4e) = 2.08 Å, B-Y(4g) = 2.79 Å and B-Y(4f) = 3.28 Å. The vertical edge lengths are Co(4e)-Co(4e) = 2.64 Å and Co(16k1)-Co(16k1) = 3.00 Å. Distances in the triangular face are Co(16k1)-Co(4e) = 2.45 Å and Co(16k1)-Co(16k1) =2.53 Å.

#### 2.2. The average Co magnetic moment

The dependence of the average magnetic moment per Co atom,  $\mu_{Co}$ , and Curie temperature, Tc, on the *B* concentration for  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 2)



*Figure 2* The dependence of the average distances from each Co site to the neighboring Co and *B* atoms,  $d_{Co-Co}$  and  $d_{Co-B}$ , and from each *B* site to the neighboring *B* atoms,  $d_{B-B}$  on the *B* concentration for  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ),  $Pr_3Co_{13}B_2$ ,  $Pr_5Co_{19}B_6$  and  $Y_2Co_{14}B$ . The density, D, of  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ),  $Y_3Co_{13}B_2$ ,  $Y_5Co_{19}B_6$  and  $Y_2Co_{14}B$  is also shown.



*Figure 3* Trigonal prism containing a boron atom in the YCo<sub>4</sub>B structure.

3 and  $\infty$ ), Pr<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Pr<sub>5</sub>Co<sub>19</sub>B<sub>6</sub> and Y<sub>2</sub>Co<sub>14</sub>B is shown in Fig. 4. The values of  $\mu_{Co}$  and Tc for YCo<sub>5</sub>, YCo<sub>4</sub>B, Y<sub>3</sub>Co<sub>11</sub>B<sub>4</sub>, Y<sub>2</sub>Co<sub>7</sub>B<sub>3</sub>, Pr<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Pr<sub>5</sub>Co<sub>19</sub>B<sub>6</sub> and Y<sub>2</sub>Co<sub>14</sub>B are from Refs. [16], [5, 17], [5, 18], [5, 19], [6], [8] and [15], respectively. The values of  $\mu_{Co}$ for Pr compounds [6, 8] are obtained by assuming that the average  $Pr^{3+}$  moment to be 2.4  $\mu_B$ . The values of  $\mu_{\rm Co}$  decrease almost linearly with increasing B concentration, that is, the values of d<sub>Co-Co</sub>. The values of Tc also decrease with increasing B concentration. Those for YCo<sub>5</sub> and Y<sub>2</sub>Co<sub>14</sub>B are large. For the other compounds, those are small and the value of  $Pr_3Co_{13}B_2$  is small comparing with those of other compounds. The dependence of the average magnetic moment per Co atom,  $\mu_{Co}$ , and Curie temperature, Tc, on the average number of the nearest neighbor Co atoms at each site, N(Co), for  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ), Pr<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Pr<sub>5</sub>Co<sub>19</sub>B<sub>6</sub> and Y<sub>2</sub>Co<sub>14</sub>B is shown in Fig. 5.



*Figure 4* The dependence of the average magnetic moment per Co atom and Curie temperature on the *B* concentration for  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ), Pr<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Pr<sub>5</sub>Co<sub>19</sub>B<sub>6</sub> and Y<sub>2</sub>Co<sub>14</sub>B.



*Figure 5* The dependence of  $\mu_{Co}$ , and Tc on the average number of the nearest neighbor Co atoms at each site, N(Co), for  $Y_{n+1}Co_{3n+5}B_{2n}$   $(n = 0, 1, 2, 3 \text{ and } \infty)$ ,  $Pr_3Co_{13}B_2$ ,  $Pr_5Co_{19}B_6$  and  $Y_2Co_{14}B$ .

The values of  $\mu_{Co}$  and Tc increase with increasing the values of N(Co). Hence, the increased N(Co) and the decreased  $d_{Co-Co}$  enhance the values of  $\mu_{Co}$  and Tc.

The concentration of the numbers of Co(0), Co(1) and Co(2) sites versus the average Co monent for  $Y_{n+1}Co_{3n+5}B_{2n}$   $(n = 0, 1, 2, 3 \text{ and } \infty)$ ,  $Pr_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 1 and m = 2, n = 3)and  $Nd_{m+n}Co_{5m+3n}B_{2n}$  (m = 3, n = 2) are shown in Fig. 6. The average Co moment increases with increasing the Co(0) concentration and decreases with increasing the Co(2) one.

2.3. A model of the moment variation in  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ),  $Pr_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 1 and m = 2, n = 3),  $Nd_{m+n}Co_{5m+3n}B_{2n}$ (m = 3, n = 2) and  $Y_2Co_{14}B$  compounds

We consider a model focus on boron coordination in explaining magnetic moments in those compounds. The



*Figure 6* The concentration of the numbers of Co(0), Co(1) and Co(2) sites versus the average Co monent for  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ),  $Pr_3Co_{13}B_2$ ,  $Pr_5Co_{19}B_6$  and  $Nd_5Co_{21}B_4$ .

extent of p-d bonding is assumed to be proportional to the number of T (transition-metal) atoms surrounding an M (metalloid) atom, Z. If the T atom is strongly ferromagnetic with a magnetization at 0 K of  $n_B$ , the magnitude of the average magnetic moment  $\mu$  per T atom in the alloy is shown as below [20]:

$$\mu = n_B - Z(n_B/5)(N_M/N_T),$$
 (1)

where  $N_M/N_T$  is the ratio of the number of M atoms to T atoms. Equation 1 assumes that each of the Z nearestneighbor T atoms forms a bond with the central M atom and therefore loses, on average, one fifth of its moment because one of its five 3d electron orbitals is tied up in a nonmagnetic, covalent bond.

We show the average Co magnetic moment,  $\mu_{Co}$ , as a function of concentration  $N_B/N_{Co}$  for  $Y_{n+1}Co_{3n+5}B_{2n}$  $(n = 0, 1, 2, 3 \text{ and } \infty)$ ,  $Pr_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 1)1 and m = 2, n = 3), Nd<sub>*m*+*n*</sub>Co<sub>5*m*+3*n*</sub>B<sub>2*n*</sub> (m = 3, n =2) and  $Y_2Co_{14}B$  compounds in Fig. 7. The values of  $\mu_{\text{Co}}$  for YCo<sub>5</sub>, YCo<sub>4</sub>B, Y<sub>3</sub>Co<sub>11</sub>B<sub>4</sub>, Y<sub>2</sub>Co<sub>7</sub>B<sub>3</sub>, YCo<sub>3</sub>B<sub>2</sub>,  $Pr_3Co_{13}B_2$ ,  $Pr_5Co_{19}B_6$ ,  $Nd_5Co_{21}B_4$  and  $Y_2Co_{14}B$  are from Refs. [16], [5], [5], [5], [5], [6], [9], [10] and [15], respectively. The values of  $\mu_{Co}$  for Pr [6, 8] and Nd [10] compounds are obtained by assuming that the average  $Pr^{3+}$  and  $Nd^{3+}$  moment to be 2.4 and 3.0  $\mu_B$ , respectively. The value of  $n_{\rm B}$  was taken as 1.72  $\mu_{\rm B}$  for hcp Co. The value of  $\mu_{Co}$  does not decrease linearly with increasing that of  $N_B/N_{Co}$ . Line a is a model in Equation 1, where Z is six, and departs from the values of  $\mu_{Co}$ . So, we must change the value of Z in Equation 1 to fit the values of  $\mu_{Co}$ . Line *B* is calculated using a least-squares program for  $0 \le N_B/N_{\rm Co} \le 0.66$  and the value of Z is 9.1, but the line does not fit the values of  $\mu_{\rm Co}$ . In all regions, a line can not be drown and there are two slopes. Next, we obtained line c using a leastsquares program for  $0 \le N_B/N_{Co} \le 0.25$ . The line fits



*Figure 7* Average Co magnetic moment as a function of concentration  $N_B/N_{C0}$  for  $Y_{n+1}Co_{3n+5}B_{2n}$   $(n = 0, 1, 2, 3 \text{ and } \infty)$ ,  $Pr_3Co_{13}B_2$ ,  $Pr_5Co_{19}B_6$ ,  $Nd_5Co_{21}B_4$  and  $Y_2Co_{14}B$  compounds. Line a is a model in Equation 1. Lines *B* and c are calculated using a least-squares program for  $0 \le N_B/N_{C0} \le 0.66$  and for  $0 \le N_B/N_{C0} \le 0.25$ , respectively.

the values of  $\mu_{Co}$  well and the value of Z is 13.2. Consequently, the value of Z is varied continuously from 13.2 for  $0 \le N_B/N_{Co} \le 0.25$  to 9.1 for  $0 \le N_B/N_{Co} \le$ 0.66. The value of Z is near 13.2 and a boron atom bonds with 13.2 Co atoms for  $Y_2Co_{14}B$ ,  $Pr_3Co_{13}B_2$ ,  $Nd_5Co_{21}B_4$  and  $YCo_4B$ . The value of Z is near 9.1 and a boron atom bonds with 9.1 Co atoms for  $Pr_5Co_{19}B_6$ ,  $Y_3Co_{11}B_4$  and  $Y_2Co_7B_3$ . Consequently, the extent of p-d bonding becomes large with decreasing the value of  $N_B/N_{Co}$  and gives rise to a sharper moment reduction. The value of Z is large comparing with that obtained from structural analysis. While we assume that T atom loses one fifth of its moment, T atom is considered to lose more its moment.

## 2.4. The magnetic properties of hypothetical $Y_{m+n}Co_{5m+3n}B_{2n}$ (n = 1, m = 2, 3, 4 and 5) compounds

The Y<sub>2</sub>Co<sub>14</sub>B compound is most similar to Pr<sub>3</sub>Co<sub>13</sub>B<sub>2</sub> among Y<sub>n+1</sub>Co<sub>3n+5</sub>B<sub>2n</sub> (n = 0, 1, 2, 3 and  $\infty$ ) and Pr<sub>m+n</sub>Co<sub>5m+3n</sub>B<sub>2n</sub> (m = 2, n = 1 and m = 2, n = 3) compounds, considering *B* concentration and Co moment. Here, increasing m from 2 to 5 with n = 1, the *B* concentration decreases and that of m = 5 is almost equal to that of Y<sub>2</sub>Co<sub>14</sub>B and the comparizon of those compounds with Y<sub>2</sub>Co<sub>14</sub>B is very interesting. Hence, we estimate the Co moment for hypothetical Y<sub>m+n</sub>Co<sub>5m+3n</sub>B<sub>2n</sub> (n = 1, m = 2, 3, 4 and 5) compounds, which are Y<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Y<sub>2</sub>Co<sub>9</sub>B, Y<sub>5</sub>Co<sub>23</sub>B<sub>2</sub> and Y<sub>3</sub>Co<sub>14</sub>B, respectively. Those are formed by alternate stacking of m parts of RCo<sub>5</sub> with one part of RCo<sub>3</sub>B<sub>2</sub> along the *c* axis. The *B* atoms reside only in the *z* = 0 and 1 planes. Those compounds have Co(0) and Co(1) sites. The values of  $\mu_{Co}$  at the 2c site, which is Co(0) site, and 6i site, which is Co(1) site, for YCo<sub>4</sub>B obtained by neutron powder diffraction are 1.5 and 0.5  $\mu_B$ , respectively [9], and we used the values. So the calculated values of  $\mu_{Co}$  are 1.0, 1.2, 1.2 and 1.3  $\mu_B$  for Y<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Y<sub>2</sub>Co<sub>9</sub>B, Y<sub>5</sub>Co<sub>23</sub>B<sub>2</sub> and Y<sub>3</sub>Co<sub>14</sub>B, respectively. The value of  $\mu_{Co}$  decreases almost linearly with increasing *B* concentration. The *B* concentration for Y<sub>2</sub>Co<sub>14</sub>B (5.88%) is almost equal to that for Y<sub>3</sub>Co<sub>14</sub>B are 1.4 and 1.3  $\mu_B$ , respectively.

Next, we estimate the magnetic anisotropy for hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (*n* = 1, *m* = 2, 3, 4 and 5) compounds. The NMR study of RCo<sub>5</sub> by Streever [21] indicated that the spin-orbit magnetic moment of Co atom at the 2c site contributes significantly to the anisotropy of RCo<sub>5</sub>. The uniaxial magnetization direction of RCo<sub>5</sub> stems from Co atoms at the 2c site and Co atoms at the 3g site exert a relatively small reverse contribution [21]. Moreover to study the Co contribution to the magnetic anisotropy, we calculate the total anisotropy energy,  $E_A$ , using the local anisotropy energy per Co atom, Es, of the hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (n = 1, m = 2, 3, 4 and 5) compounds, which are Y<sub>3</sub>Co<sub>13</sub>B<sub>2</sub>, Y<sub>2</sub>Co<sub>9</sub>B, Y<sub>5</sub>Co<sub>23</sub>B<sub>2</sub> and Y<sub>3</sub>Co<sub>14</sub>B, respectively. We used the values of Es in YCo<sub>5</sub> [21] and Y<sub>3</sub>Co<sub>11</sub>B<sub>4</sub> [22]. In YCo<sub>5</sub>, the values of Es at the 2c and 3g sites, being Co(0) site, are 24 and  $-7 \text{ cm}^{-1}$ /atom, respectively. In YCo<sub>5</sub>, the net calculated anisotropy energy is 27 cm<sup>-1</sup>/unit cell or about  $6.4 \times 10^7$  erg/cm<sup>3</sup>. This is close to the measured low temperature anisotropy energy  $K_1$  of  $7.5 \times 10^7$  $erg/cm^{3}$  for YCo<sub>5</sub> [23]. It appears then that the singleion anisotropy could explain most of the anisotropy of the compound [24]. In  $Y_3Co_{11}B_4$ , the values of Es at the 6i1 site, being Co(1) site, and the 6i2 site, being Co(2) site, are -8.1 and 0.69 cm<sup>-1</sup> /atom, respectively. Then

$$E_{A}(Y_{3}Co_{13}B_{2}) = 3Es(3g) + 4Es(4h) + 6Es(6i)$$
  
= 26.4 cm<sup>-1</sup>/unit cell, (2)

where Es(4h) = Es(2c) and Es(6i) = Es(6i1). The calculated values of  $E_A$  for  $Y_2Co_9B$ ,  $Y_5Co_{23}B_2$  and  $Y_3Co_{14}B$  are 53.4, 80.4 and 107.4 cm<sup>-1</sup>/unit cell, respectively.

Similarly, the calculated values of  $E_A$  for hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 3 and m = 3, n = 2) compounds, which are  $Y_5Co_{19}B_6$  and  $Y_5Co_{21}B_4$ , are -1.2 and 46.8 cm<sup>-1</sup>/unit cell, respectively. The dependence of the value of  $E_A$  and the average Es on the *B* concentration for hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (n = 1, m = 2, 3, 4 and 5), hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 3 and m = 3, n = 2) and  $Y_2Co_{14}B$  [25] compounds is shown in Fig. 8. The average Es decreases with increasing *B* concentration except for that of  $Y_2Co_{14}B$ .

The easy magnetization direction in  $Pr_3Co_{13}B_2$  from 5 K to room temperature is parallel to the *c* axis [6]



*Figure 8* The dependence of the value of  $E_A$  and the average Es on the *B* concentration for hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (n = 1, m = 2, 3, 4 and 5), hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 3 and m = 3, n = 2) and  $Y_2Co_{14}B$  compounds.

and is explained as below. In  $R_{m+n}Co_{5m+3n}B_{2n}$ , the sign of  $A_2^0$  is negative [3], which means that the R ion having a negative second-order Stevens coefficient  $\alpha_J$  (Pr<sup>3+</sup>, Nd<sup>3+</sup>) shows planar anisotropy. The magnetic anisotropy results from a competition between the planar anisotropy of the Pr ions and the uniaxial one of the Co sublattice. The axial anisotropy of Co atoms is large, hence the Pr<sub>3</sub>Co<sub>13</sub>B<sub>2</sub> compound has axial anisotropy. In  $R_{m+n}Co_{5m+3n}B_{2n}$ , the *R* ion having a positive  $\alpha_I$  (Sm<sup>3+</sup>) shows axial anisotropy. The magnetic anisotropy of R in the plane containing B atoms is strengthened by B atoms as explained below. The Ratom is surrounded by B atoms in the c plane. Assuming that B atom has a negative charge, the 4f electrons in R atom are distributed avoiding B atoms. From the schematic distributions of the wave functions of the 4f electrons in Sm, the axial anisotropy strengthens. Consequently, the  $Sm_{m+n}Co_{5m+3n}B_{2n}$  compounds with large *B* concentration are expected to have large axial anisotropy.

#### 3. Conclusions

In this work, we estimate the average Co magnetic moment and account for the moment variation by a model in  $Y_{n+1}Co_{3n+5}B_{2n}$  (n = 0, 1, 2, 3 and  $\infty$ ),  $Pr_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 1 and m = 2, n = 3),  $Nd_{m+n}Co_{5m+3n}B_{2n}$  (m = 3, n = 2) and  $Y_2Co_{14}B$  compounds. And we obtain the magnetic properties of hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (n = 1, m = 2, 3, 4 and 5) compounds.

(1) The values of  $d_{\text{Co-Co}}$  and  $d_{\text{Co-B}}$ , the average distances from each Co site to the neighboring Co and *B* atoms, increase with increasing *B* concentration.

(2) The values of  $\mu_{Co}$  decrease almost linearly with increasing *B* concentration, that is, the values of  $d_{Co-Co}$ . The values of Tc also decrease with increasing *B* concentration. The values of  $\mu_{Co}$  and Tc increase with increasing the values of N(Co), the average

number of the nearest neighbor Co atoms at each site.

(3) The extent of p-d bonding becomes large with decreasing the value of  $N_{\rm B}/N_{\rm Co}$ , the ratio of the number of *B* atoms to Co atoms and gives rise to a sharper moment reduction.

(4) The *B* concentration for Y<sub>2</sub>Co<sub>14</sub>B is almost equal to that for hypothetical Y<sub>3</sub>Co<sub>14</sub>B. The value of  $\mu_{Co}$  is 1.4  $\mu_{B}$  for Y<sub>2</sub>Co<sub>14</sub>B and the calculated value of  $\mu_{Co}$  is 1.3  $\mu_{B}$  for Y<sub>3</sub>Co<sub>14</sub>B.

(5) The average Es decreases with increasing *B* concentration for hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (n = 1, m = 2, 3, 4 and 5) and hypothetical  $Y_{m+n}Co_{5m+3n}B_{2n}$  (m = 2, n = 3 and m = 3, n = 2) compounds.

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